

# Gravimetric Water Vapor Permeability of Flat Materials and Finished Objects

## Beyond Certification Under ISO 17025

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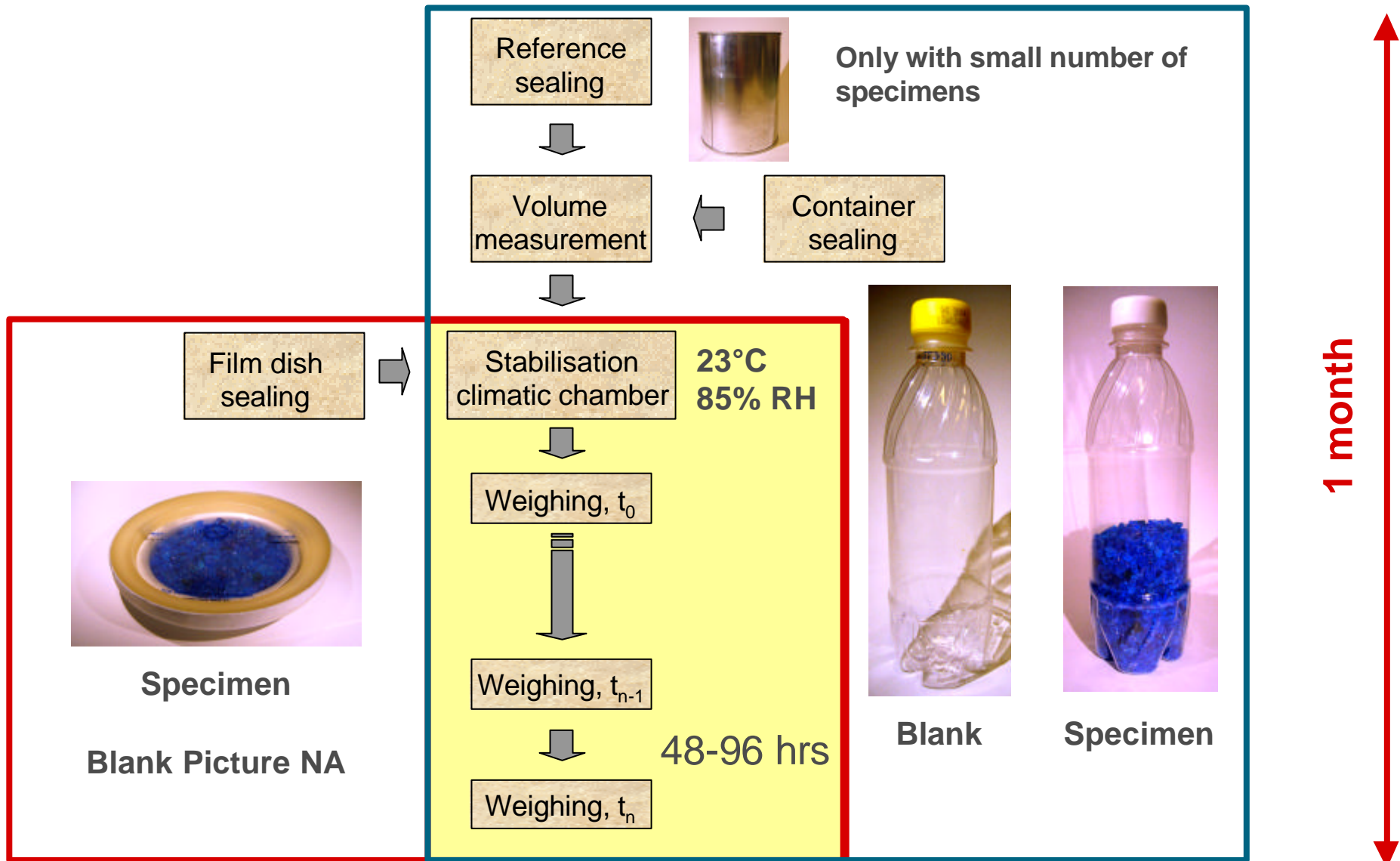
- Show dominant contributions to gravimetric WVTR uncertainty, depending on measurement procedure and measured barrier properties
- Limitations of the current method
- NOT discuss all contributions in detail

- WV-TR Method description
- Uncertainty: Causes & Relevant Effects
- Implications & Next steps

# Samples

Vapor Barrier	Film	Rigid containers
HIGH	Metallized PET	Jar Co-E-P/EVOH/Co-E-P 
LOW	Pure PET	Beverage bottle PET/MXD-6/PET 

# Method Flow Chart



# The WVTR mathematical expression does not account for all sources of uncertainty



Method	Rigid container [mg/pack.day] Flexible film [g/m <sup>2</sup> .day]	
Blank (Films & Containers)	$WVTR = \frac{(m_n - m_{n-1}) - \left[ (m_n^b - m_{n-1}^b) \right]}{A(t_n - t_{n-1})}$	Buoyancy Driving force Wall H <sub>2</sub> O content
Reference vol. (Only Containers)	$WVTR = \frac{(m_n - m_{n-1}) - \left[ (m_n^r - m_{n-1}^r) (V_s / V_r) \right]}{(t_n - t_{n-1})}$	Buoyancy

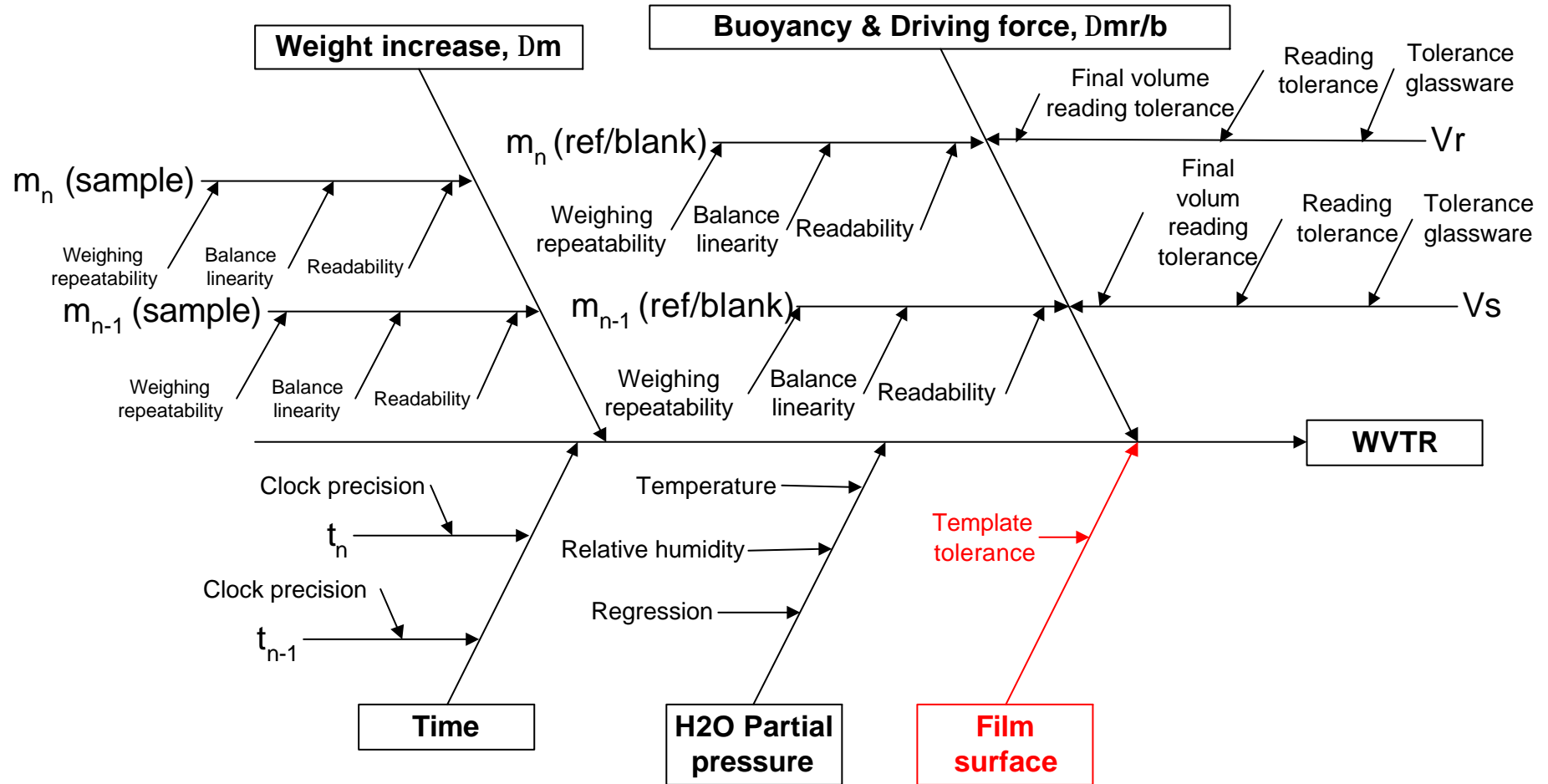
m = specimen mass [mg,g]  
 m<sup>b</sup> = blank weight [mg,g]  
 m<sup>r</sup> = reference weight [mg,g]

t = time [days]  
 V<sub>s</sub> = sample volume [cm<sup>3</sup>]  
 V<sub>r</sub> = reference volume [cm<sup>3</sup>]  
 A = film surface area [m<sup>2</sup>]



- WV-TR Method description
- **Uncertainty: Causes & Relevant effects**
- Implications & Next steps

# Cause & Effect Diagram





# Weight change $\Delta m / \Delta t$ , $\Delta m_{b,r} / \Delta t$

$$\frac{\Delta m}{\Delta t} = \frac{(m_n - m_{n-1})}{(t_n - t_{n-1})}$$

$$u_{\text{linearity}} = 0.001\text{g}$$

$$u_{\text{readability}} = 0.0002\text{g}$$

Sample (average of several specimens)

Repeatability  $\Delta m / \Delta t$

$$u(\Delta m / \Delta t) = \frac{1}{\Delta t} \sqrt{SD_{\text{rep}}^2 + 2 * \left( (u_{\text{linearity}})^2 + (u_{\text{readability}})^2 \right)}$$

Reference/blank (one specimen)

$$u(\Delta m_{r,b} / \Delta t) = \frac{1}{\Delta t} \sqrt{2 * \left( (SD_{\text{Balancerep}})^2 + (u_{\text{linearity}})^2 + (u_{\text{readability}})^2 \right)}$$

# Driving force is H<sub>2</sub>O Partial pressure not RH

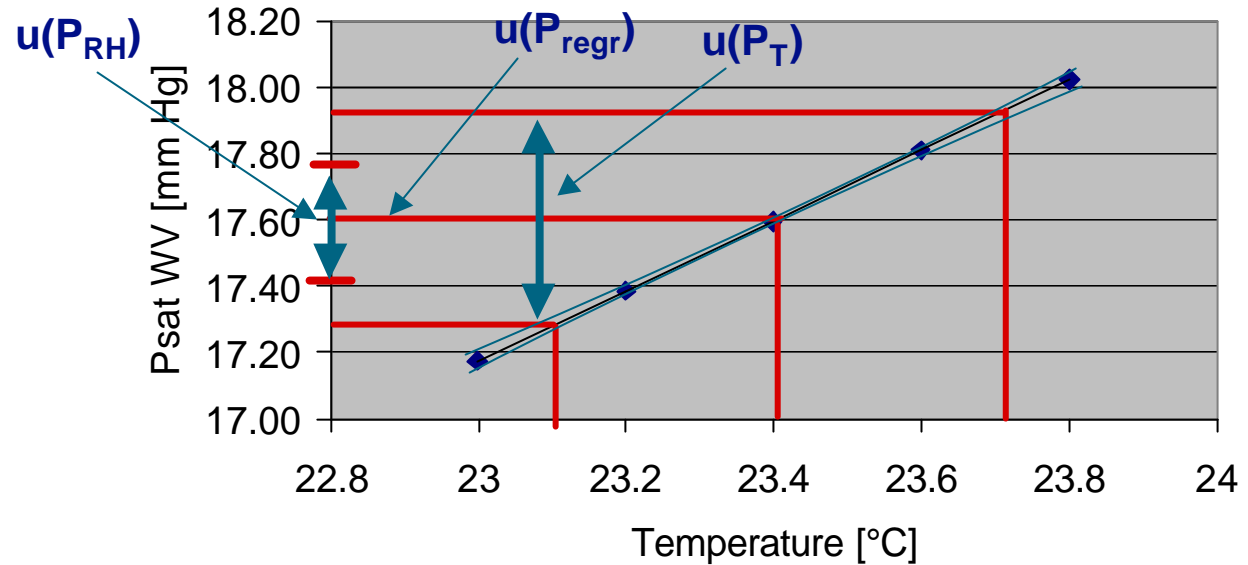
## Climate

$T = 23.4$   
 $u(T) = 0.3 \text{ } ^\circ\text{C}$   
 $RH = 81.5$   
 $u(RH) = 0.8 \text{ \%RH}$

## Driving force

$F \star (P_{\text{ext}} - P_{\text{int}})$   
 $P_{\text{int}} = 0$   
 $P_{\text{ext}} = f(T, RH)$

$$u(P_{RH}) = u(RH) * 17.56$$

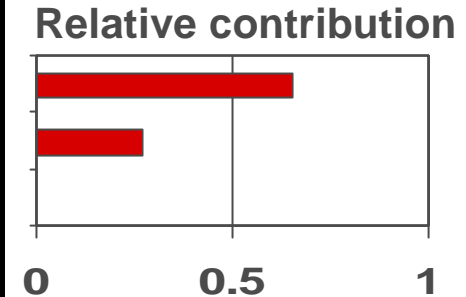


Source	$u_j$	$u_j^2$	Rel contrib.
$u(P_{\text{regr}})$	0.0008	7.0E-07	5.5E-06
$u(P_T)$	0.31	0.095	0.75
$u(P_{RH})$	0.18	0.032	0.25
<b>S (<math>u_j^2</math>)</b>		<b>0.127</b>	
<b><math>u_p</math></b>	<b>17.56</b>	<b>0.36</b>	
<b>Rel <math>u_p</math></b>	<b>1</b>	<b>0.02</b>	

# Combined Uncertainty: Films

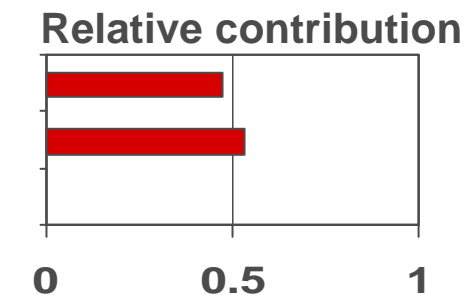
## PET (low barrier)

Source	Value	uj	ci	(ujci) <sup>2</sup>	urel
$\Delta m/\Delta t$	0.04	0.0022	199.9	0.2014	0.70
$\Delta mb/dt$	0.00	0.0015	-199.9	0.0851	0.30
<b>A</b>	<b>0.005</b>	<b>0.00001</b>	<b>-1526.7</b>	<b>0.0005</b>	<b>0.00</b>
<b>Total (ciuj)<sup>2</sup></b>				<b>0.287</b>	<b>1.00</b>
<b>Total (ciuj) [g/m<sup>2</sup>.day]</b>	<b>7.64</b>			<b>0.54</b>	
<b>Relative (ciuj)</b>				<b>0.07</b>	



## Met-PET (high barrier)

Source	Value	uj	ci	(ujci) <sup>2</sup>	urel
$\Delta m/\Delta t$	0.0017	0.0014	199.9	0.074	0.47
$\Delta mb/dt$	-0.0006	0.0015	-199.9	0.085	0.53
<b>A</b>	<b>0.005</b>	<b>0.00001</b>	<b>-92.3</b>	<b>0.000</b>	<b>0.00</b>
<b>Total (ciuj)<sup>2</sup></b>				<b>0.159</b>	<b>1.00</b>
<b>Total (ciuj) [g/m<sup>2</sup>.day]</b>	<b>0.46</b>			<b>0.40</b>	
<b>Relative (ciuj)</b>				<b>0.86</b>	

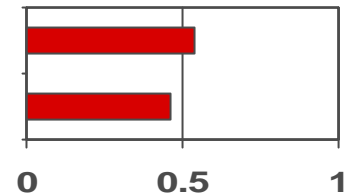


# Combined Uncertainty: Rigid containers & Blank

## Bottle (low barrier)

Source	Value	uj	ci	(ujci) <sup>2</sup>	urel
$\Delta m/\Delta t$	21.74	0.161	1	0.0258	0.54
$\Delta mb/dt$	0.29	0.147	-1	0.0217	0.46
<b>Total (ciuj)<sup>2</sup></b>				<b>0.047</b>	<b>1.00</b>
<b>Total (ciuj) [mg/pack.day]</b>	<b>21.45</b>			<b>0.22</b>	
<b>Relative (ciuj)</b>				<b>0.01</b>	

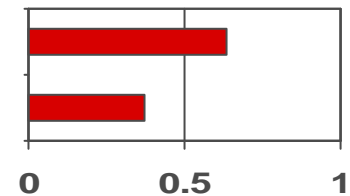
Relative contribution



## Jar (high barrier)

Source	Value	uj	ci	(ujci) <sup>2</sup>	urel
$\Delta m/\Delta t$	1.21	0.190	1	0.0363	0.63
$\Delta mb/dt$	0.43	0.147	-1	0.0217	0.37
<b>Total (ciuj)<sup>2</sup></b>				<b>0.058</b>	<b>1.00</b>
<b>Total (ciuj) [mg/pack.day]</b>	<b>0.79</b>			<b>0.24</b>	
<b>Relative (ciuj)</b>				<b>0.31</b>	

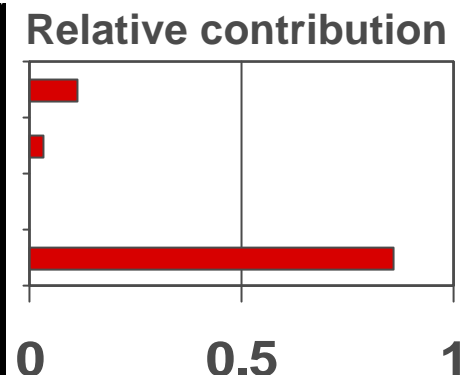
Relative contribution



# Combined Uncertainty: Rigid containers & Reference Volume

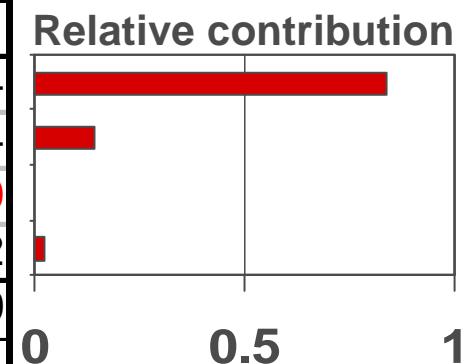
## Bottle (low barrier)

Source	Value	uj	ci	(ujci) <sup>2</sup>	urel
$\Delta m/\Delta t$	21.74	0.161	1	0.0258	0.11
$\Delta mr/dt$	-0.21	0.149	-0.53	0.0061	0.03
Vs/Vr	0.53	0.026	-0.21	0.0000	0.00
P H2O	1	0.02	21.85	0.1964	0.86
<b>Total (ciuj)<sup>2</sup></b>				<b>0.228</b>	<b>1.00</b>
<b>Total (ciuj) [mg/pack.day]</b>	<b>21.85</b>			<b>0.48</b>	
<b>Relative (ciuj)</b>				<b>0.02</b>	

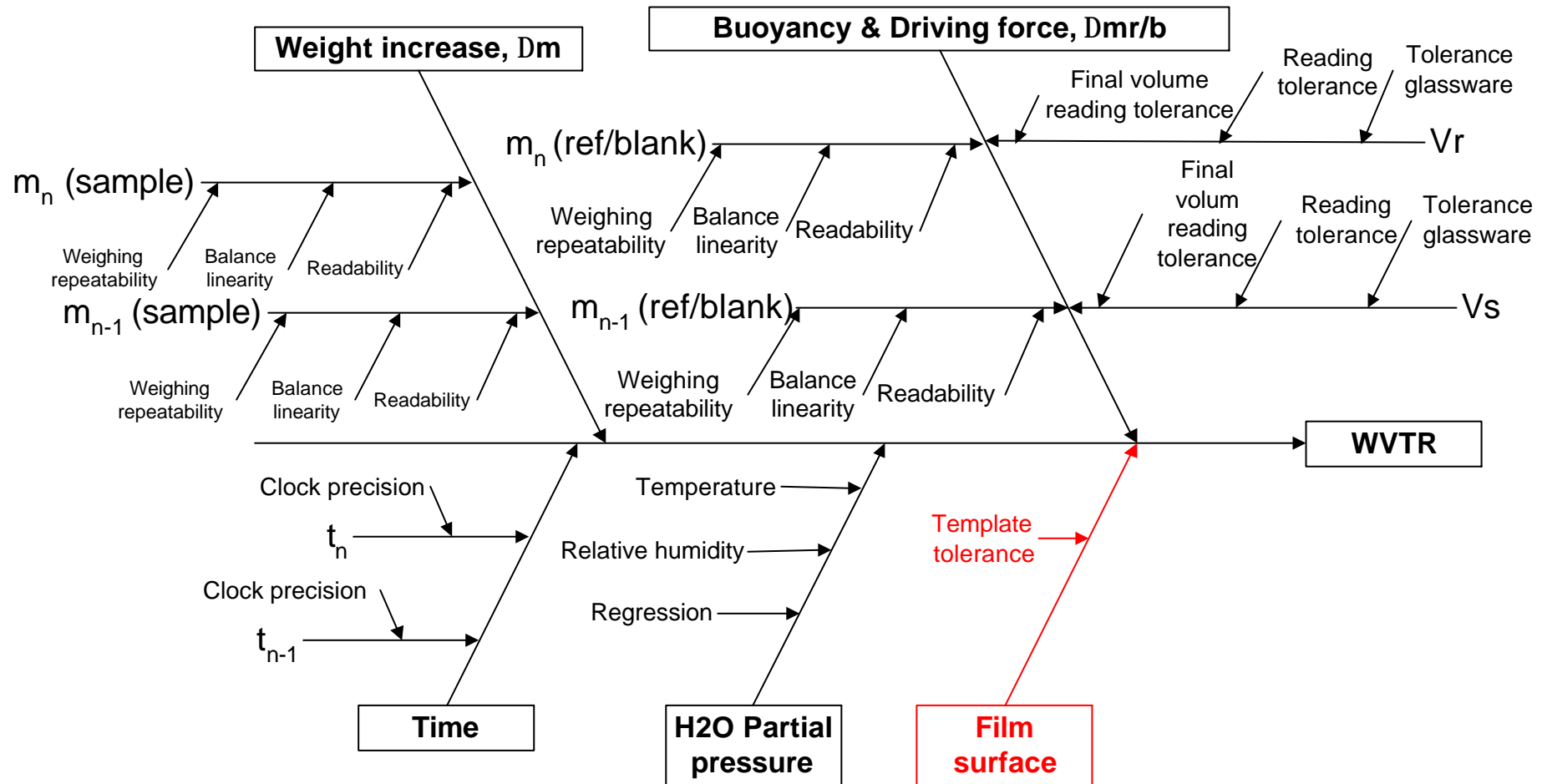


## Jar (high barrier)

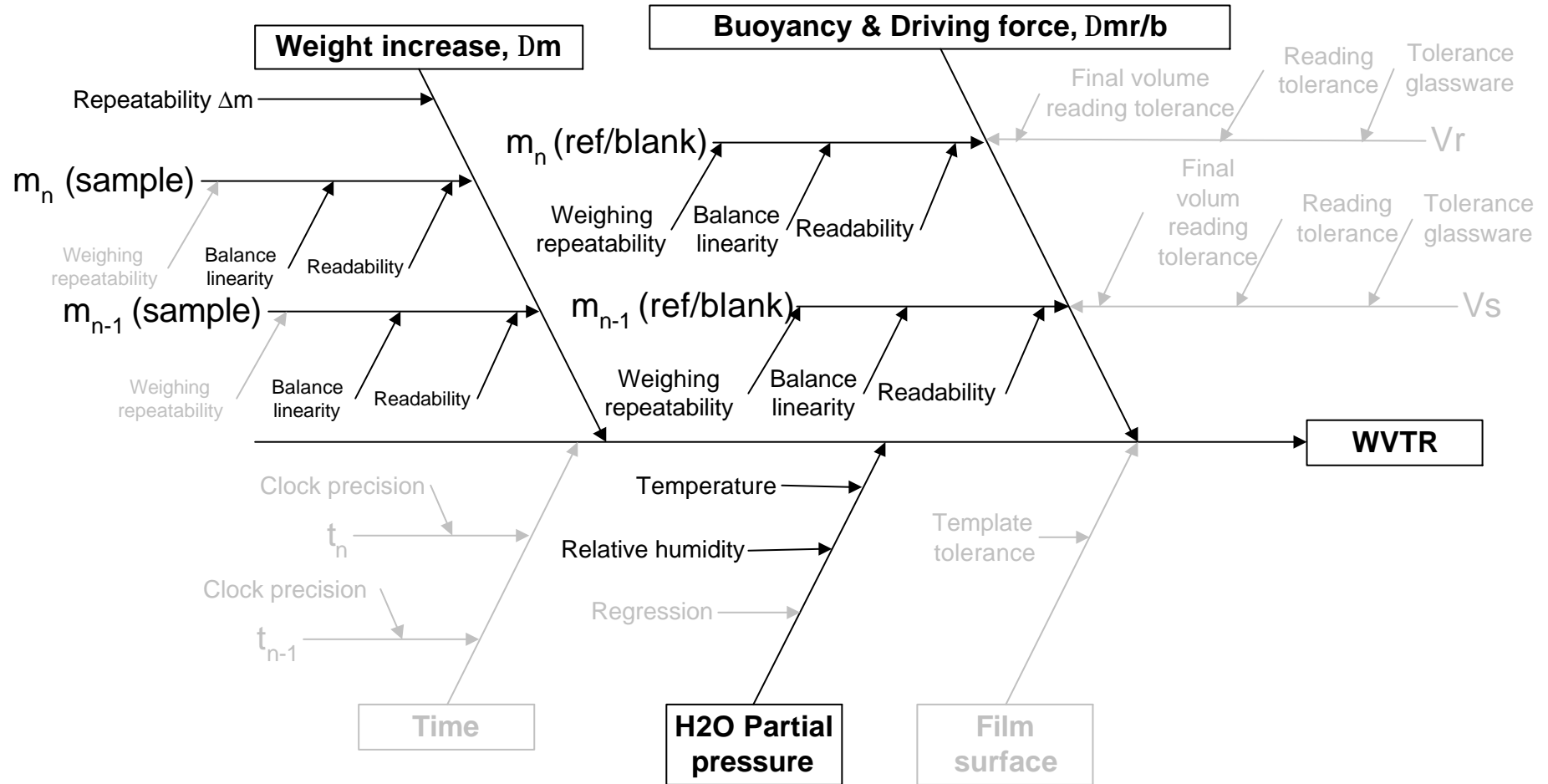
Source	Value	uj	ci	(ujci) <sup>2</sup>	urel
$\Delta m/\Delta t$	1.21	0.190	1	0.0363	0.84
$\Delta mr/dt$	-0.21	0.149	-0.52	0.0060	0.14
Vs/Vr	0.520	0.026	-0.21	0.0000	0.00
P H2O	1	0.02	1.32	0.0007	0.02
<b>Total (ciuj)<sup>2</sup></b>				<b>0.043</b>	<b>1.00</b>
<b>Total (ciuj) [mg/pack.day]</b>	<b>1.32</b>			<b>0.21</b>	
<b>Relative (ciuj)</b>				<b>0.16</b>	



# Cause & Effect Diagram



# Refined Cause & Effect Diagram



# Expanded Uncertainty Containers: Reference gives different result for low barriers



Barrier	Method	Value	Expanded uncertainty (k=2)	Comparison of means & variances 5% significance
LOW	Blank	21.45	0.98	NOT DIFFERENT
	Reference	21.85	0.96	
HIGH	Blank	0.79	0.48	DIFFERENT!
	Reference	1.32	0.42	





- WV-TR Method description
- Uncertainty: Causes & Relevant Effects
- **Implications & Next steps**

- Present method suited for low to medium barrier applications
  - MU for intermediate barriers
- Reference volume should be used with caution for medium to low barrier materials
- For reference volume method the climate control dominates uncertainty for low barriers, while remaining significant for high barriers
- Method improvement
  - Increase time-span between weighing not possible
  - Use balance with higher sensitivity
  - Linear regression over several measurements

# Film surface area, A

$$D = 79.8 \pm 0.2 \text{ mm}$$

$$c_D = \frac{\partial}{\partial D} \left( \frac{\rho D^2}{4} \right) = \frac{\rho D}{2}$$

A [m <sup>2</sup> ]	interval	distribution	uj	ci	ciuj
0.005	0.0002	rectangular	0.000115	0.12535	1.45E-05
				<b>Urel</b>	<b>0.003</b>

# Sample volume/reference volume



## Uncertainty of one volume measurement

Source	interval	distribution	uj	ci	ciuj	(ciuj)^2	urel
filling	20	rectangular	11.5	1	11.5	133	0.25
reading	20	rectangular	11.5	1	11.5	133	0.25
line marking	28	rectangular	16.2	1	16.2	261	0.49
<b>Total (ciuj)^2</b>						<b>528</b>	<b>1.00</b>
<b>Total (ciuj)</b>						<b>23.0</b>	

Expression

$$\frac{V_s}{V_r}$$

Sensitivity coefficients (ci) for combined uncertainty

$$\frac{\partial \left( \frac{V_s}{V_r} \right)}{\partial V_s} = \frac{1}{V_r} \quad \frac{\partial \left( \frac{V_s}{V_r} \right)}{\partial V_r} = -\frac{V_s}{V_r^2}$$

Combined uncertainty beverage bottle, u(V)

Source	Value	uj	ci	(ujci)^2	urel
Vs	525	23.0	0.001	0.00053	0.78
Vr	1000	23.0	-0.000525	0.00015	0.22
<b>Tot (ujci)^2</b>				<b>0.001</b>	
<b>Tot (ujci)</b>	<b>0.525</b>			<b>0.026</b>	
<b>Rel u(V)</b>				<b>0.049</b>	

